

Article

# $(\mathcal{C}, \Psi^*, G)$ Class of Contractions and Fixed Points in a Metric Space Endowed with a Graph

Reny George <sup>1,2,\*</sup>, Ekta Tamrakar <sup>3</sup>, Jelena Vujaković <sup>4</sup>, Hemant Kumar Pathak <sup>3</sup> and Selvavinayagam Velusamy <sup>5</sup>

<sup>1</sup> Department of Mathematics, College of Science, Prince Sattam bin Abdulaziz University, Al-Kharj 11942, Saudi Arabia

<sup>2</sup> Department of Mathematics and Computer Science, St. Thomas College, Bhilai, Chhattisgarh 490006, India

<sup>3</sup> School of Studies in Mathematics, Pt. Ravishankar Shukla University, Raipur (C.G.) 492010, India; tamrakarekta@gmail.com (E.T.); hkpathak05@gmail.com (H.K.P.)

<sup>4</sup> Faculty of Sciences and Mathematics, University of Privstina, Kosovska Mitrovica 38220, Serbia; jelena.vujakovic@pr.ac.rs

<sup>5</sup> Nasser Vocational Training Centre, Jau, Kingdom of Bahrain; selvavinayakam.v@gmail.com

\* Correspondence: renygeorge02@yahoo.com

Received: 18 April 2019; Accepted: 17 May 2019; Published: 27 May 2019



**Abstract:** In this paper, we introduce the  $(\mathcal{C}, \Psi^*, G)$  class of contraction mappings using  $\mathcal{C}$ -class functions and some improved control functions for a pair of set valued mappings as well as a pair of single-valued mappings, and prove common fixed point theorems for such mappings in a metric space endowed with a graph. Our results unify and generalize many important fixed point results existing in literature. As an application of our main result, we have derived fixed point theorems for a pair of  $\alpha$ -admissible set valued mappings in a metric space.

**Keywords:** fixed point; common fixed point; directed graph; edge preserving; transitivity property

**MSC:** 47H10; 54H25